

LETTER

## Mind Model Seems Necessary for the Emergence of Communication

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**Abstract**—We consider communication when there is no agreement about symbols and meanings. We treat it within the framework of reinforcement learning. This framework enables us to talk about emotional coupling and to consider the emergence of communication. We apply different reinforcement learning models in our studies and simplify the problem as much as possible. We show that the modelling of the other agent is insufficient in the simplest possible case, unless the intentions can also be modelled. The model of the agent and its intentions enable quick agreements about symbol-meaning association. We show that when both agents assume an ‘intention model’ about the other agent then the symbol-meaning association process can be spoiled and symbol meaning association may become hard.

**Keywords**—Emotion, theory of mind, decision making, reinforcement, learning

### 1. Introduction

The emergence of communication is one of the most enigmatic problems for several disciplines including evolution, natural language theory, information technology. For a recent collection of papers, see, e.g., [2]. For proper treatment, the concept of communication needs to be considered. First, let us see a few examples.

*Smoke signals.* These are ‘few bit’ signals that could mean attention, danger, help, and so on. The vocabulary is small, the communication speed is high, the communication distance is large. The primary goal of this communication is to overcome limited observation capabilities of other agents, to warn, and to coordinate future actions.

*Atomic interactions.* Not all light enabled interaction is, however, communication: Atoms, for example, interact each other by exchanging photons. The emission and the absorption of photons are not intentional and the transmitted photon has no hidden meaning.

*Grooming.* According to Dunbar, grooming between monkeys is used, for example, to form alliances, serve, or apologize [3]. Thus, we consider grooming communication, although it is non-verbal communication.

Then, the common features of communication are as follows: (i) communication is optional, (ii) it is intentional, and (iii) communicated signals are symbols of certain meanings. Further, (iv) communication is successful, if the meaning is the same for those who communicate. The emergence of communication is the subject of evolutionary linguistics (for a recent review on evolutionary linguistics, see [12]). Evolutionary linguistics focuses on the selective scenario that might give rise to the appearance of early languages. There are many theories and many possibilities. Let us consider the popular and efficient language game approach [13, 10, 9, 8]. In language games, the theoretical approach makes certain assumptions. Presupposed conditions include the following: agents interact and their interaction is ‘coordinated’. Thus, language game presupposes the existence of an agreement that agents start to engage themselves in ‘coordinated actions’. Such an agreement is also a symbol-meaning association. Thus, the language game approach assumes existing symbol-meaning association and builds on that assumption.

Our question concerns the very minimum of symbol-meaning association needed for successful communication. To this end, we make the problem as simple as possible. Our analysis is embedded into the framework of

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reinforcement learning. We study how communication may depend on the presence or the absence of the communication of emotions or internal *values*. In our simulations, communication will emerge as a deliberate action of the agents, but only if certain conditions are fulfilled.

The paper is organized as follows. We provide the theoretical analysis in Section 2. This analysis shows the necessity of emotional coupling between agents. We illustrate the analysis with simulations in simple scenarios (Section 3). We shall discuss our results in Section 4. We conclude in Section 5. The paper is understandable without involved mathematical tools. Mathematical details are presented in the Appendices for the sake of completeness.

## 2. Theoretical Analysis

In this section, we investigate conditions when communication between two autonomous agents can *emerge*. The question is, how two autonomous agents could learn to communicate? We assume that neither the meanings nor the communication signals are fixed in advance, there is no special method of negotiation, and there is no *will* for communication. However, the possibility for communication is given, and the world is such that communication could be advantageous.

We investigate the problem in the framework of *reinforcement learning* (for an excellent introduction, see [11]). We investigate how communication may emerge from *joint* problem solving. That is, we ask how agents could learn when and what to communicate based on utility; how they could learn to emit and interpret signals provided that both parties benefit from those. It is surprising that if communication has a cost, then it is still not sufficient that

- the possibility of communication is given and
- communication would be beneficial for both agents (even with costs).

The underlying reason is that we have assumed that none of the agents has fixed an interpretation of the signals, therefore they have to learn *simultaneously* the translation from meanings to signals and vice versa. Let us call one of the agents, that wishes to communicate something the ‘speaker’, and the other one, which should learn to interpret it, the ‘listener’. Now consider the case, when both agents are in the learning phase, and the speaker experiments with different signals to express different meanings. The listener may not be able to differentiate the meanings, and because of the costs, stops listening (i.e. learns that it is not worth to communicate). This effect appears already in the simplest possible case. In this case, behaviors can be computed analytically.

### 2.1 A simple communication scenario

Consider two agents, *A* and *B*. For the sake of simplicity, we assume that communication is one-directional: *A* may speak and *B* may listen to it. In each episode, agent *A* may either be in state "1" or "2" (with equal probability), and has three possible actions: communicate "X", communicate "Y", and do not communicate. Communication has a cost of  $1 > c_A \geq 0$ . Agent *B* may listen to the signal of *A* for a cost of  $1 > c_B \geq 0$ , and has to guess the state of *A* (say "1" or "2"). They both receive a reward of +1, if the guess is correct and a penalty of -1 if not. Since the cost of communication is less than the reward obtainable by it, communication is desirable, if the two agents are able to agree that saying "X" means one of the states and saying "Y" means the other.

**Parametrization of the symbol-meaning association:** The policy of *A* can be described by the triple  $M_A = (\alpha, p_1, p_2)$ , where  $\alpha$  is the probability that *A* will communicate something,  $p_1$  is the probability that *A* says "X" in state "1",  $1 - p_1$  is the probability that *A* says "Y" in state "1" given that he decides to communicate, and  $p_2$  is the probability that *A* says "X" in state "2",  $1 - p_2$  is the probability that *A* says "Y" in state "2" given that he is communicating. Similarly, the policy of *B* can be described by the triple  $M_B = (\beta, q_X, q_Y)$ , where  $\beta$  is the probability that *B* will listen to the signal,  $q_X$  is the probability that *B* guesses "1" after hearing "X",  $1 - q_X$  is the probability that *B* guesses "2" after hearing "X" given that he listens, and  $q_Y$  is the probability that *B* guesses "1" after hearing "Y",  $1 - q_Y$  is the probability that *B* guesses "2" after hearing "Y" given that he listens. The probabilities and rewards for the case when *A* talks and *B* listens are summarized in Figure 1. If *B* does not listen, or *A* does not talk, then *B* guesses "1" with probability 0.5.

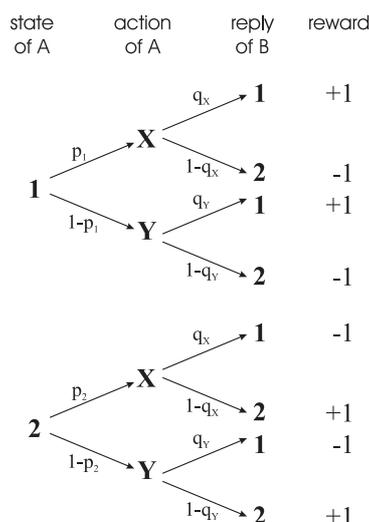


Figure 1. Various outcomes and associated rewards

**The value functions:** It is easy to calculate, that if both of them communicate, the common part of their expected reward is  $(p_1 - p_2)(q_X - q_Y)$ , and 0 if any of them is not communicating. Thus, the expected reward for policies  $M_A$  and  $M_B$  is

$$R_A(M_A, M_B) = \alpha \cdot (-c_A) + 2\alpha\beta(p_1 - p_2)(q_X - q_Y)$$

for agent  $A$  and

$$R_B(M_A, M_B) = \beta \cdot (-c_B) + 2\alpha\beta(p_1 - p_2)(q_X - q_Y).$$

for agent  $B$ .

## 2.2 Reinforcement learning of association models

Reinforcement learning aims to solve behavior optimization based on immediate rewards. The main goal of optimization is to maximize the long-term discounted and cumulated reward, the *value*, or *return* during the decision making process. Reinforcement learning problems may be solved by value function estimation or by direct strategy (policy) search methods. In *value function estimation*, states or state-action pairs are assigned value estimates that reflect the expected value of the long term cumulated and possibly discounted reward of choosing them. The agent is not greedy and may not choose the optimal immediate reward, but it tries to act greedily according to this value function: he selects the next state or action, which promises the optimal long-term (discounted and) cumulated reward also called *return*.

It is known that in partially observed environment, like in our case when the internal states of the agents may not be observed, the *direct policy search* method can be more efficient [1]. In this case, the policy of the agent is explicitly represented in a parameterized form, and the parameters are updated so that the described policy becomes optimal from the point of view of the *return*. Policy gradient methods maximize the expected *return* by using gradient methods. The gradient of the *return function* can be calculated explicitly if the return function is known (see Appendix 6.1). However, general methods also exist for cases when the reward function is not known explicitly (Appendix 6.2).

**Difficulties of parallel learning:** We have assumed that neither  $A$  nor  $B$  can bind meanings to signals, so initially  $p_1 \simeq p_2$  and  $q_X \simeq q_Y$ . Let us investigate the learning process of agent  $A$ . If  $|q_X - q_Y| < \varepsilon$  ( $B$  cannot distinguish well between meanings), the cost term of  $A$  will be greater than his reward term, so (i) he cannot tune  $p_1$  and  $p_2$  reliably (their gradient is small), and (ii) he can minimize his losses by lowering  $\alpha$ . The exact value of  $\varepsilon$  depends on the cost of communication. Similarly,  $B$  will try to minimize  $\beta$  until  $A$  does not learn to distinguish between concepts, and cannot reliably tune  $q_X$  and  $q_Y$ .

As a result, during early trials,  $p_1, p_2, q_X$  and  $q_Y$  can only change stochastically, by random walk. As the cost of communication grows, so does  $\varepsilon$ , and the time needed to exceed this limit by random walk grows exponentially.

However, during this time,  $\alpha$  and  $\beta$  keep diminishing. So by the time  $A$  and  $B$  could (by chance) break the symmetry, and learn the distinction of meanings, they will learn that communication is not useful. We note that in the general case, knowing the other *agent's dynamics* (the parameter sets  $(p_1, p_2, \alpha)$  and  $(q_X, q_Y, \beta)$ ) does not always help; e.g., if the reward of one agent is not available to the other agent and vice versa, or, if the rewards of the agents do not depend on each other's behaviors. In our two-state example behaviors are coupled. Then, in theory, agents could use certain methods to estimate the hidden reward function of the other agent. For example, non-direct implicit estimation is accomplished by the general policy gradient method: this method – up to some extent – overcomes partial observations. It is so, because individual trajectories are considered in this case. Successful estimation is, however, highly improbable in sophisticated real life situations.

### 2.3 Main hypothesis

Within the framework of reinforcement learning, we have a single means to cure the flaw described previously; the agents should be able to model each other's *intentions*; the dynamics and the 'goals' of the other agent. This is possible if the values  $R_A$  and/or  $R_B$  are made available to them.

Now, the situation becomes different: agent  $A$  can optimize  $M_A$  for a fixed  $M_B$ . Although agent  $A$  cannot modify the policy of  $B$ , he can model, what would be rewarding for agent  $B$ . Furthermore, he considers the optimal combination of the  $M_A$  and  $M_B$  strategies. Let us see the possible scenarios:

**One-step modelling:** Optimizing  $M_A$  for a fixed  $M_B$  means calculating the conditional strategy

$$M_{A|B}(M_B) = \arg \max_{M_A} R_A(M_A, M_B),$$

that is,  $A$  can calculate, that if  $B$  followed  $M_B$ , what would be the optimal choice for himself, i.e., for  $A$ . (For further mathematical details, see Appendix 6.3)

**Two-step modelling:** If agent  $A$  'knows' that he is using the conditional *one-step modelling* strategy about agent  $B$ , then he might as well suppose that  $B$  does the same, i.e., agent  $A$  might suppose that the strategy of agent  $B$  is the following:

$$M_{B|A}(M_A) = \arg \max_{M_B} R_B(M_A, M_B),$$

Now, agent  $A$  can simply choose his optimal strategy:

$$M_A^* = \arg \max_{M_A} R_A(M_A, M_{B|A}(M_A)).$$

It might be worth noting that this abstract problem phrasing goes beyond the problem of communication; it is a general learning problem. If an agent does something and it is visible to the other agent then it is a signal, which is dependent on the state of the first agent. If both agents are learning, then the situation becomes similar to our simplified example on communication. (For further mathematical details, see Appendix 6.4)

Here, we shall present numerical results for these methods. Note that in our simplified problem the immediate reward and the long-term reward are identical. More sophisticated situations were also studied and they show the same phenomena.

## 3. Computer Experiments

We have tested our theoretical analysis by conducting numerical experiments. We used policy gradient methods, and various methods where the agents modelled each other. We studied the following cases:

**Method 1:** The agents did not model each other. In this case we studied value based methods and *explicit policy gradient method*. We present results for *explicit policy gradient method*.

**Method 2:** The agents did not model each other directly, but use the *general policy gradient method*. This method models the world and thus the other agent implicitly.

**Method 3:** Agent  $A$  estimated agent  $B$ 's dynamics, i.e. the parameters that determine  $B$ 's policy. In this case, agent  $A$  used a one-step model of agent  $B$ . Thus, in this model, agent  $A$  *senses* the rewards of agent  $B$  and

chooses the optimal policy accordingly. Agent *B* did not model agent *A* and applied the policy gradient method

**Method 4:** Both agent *A* and agent *B* had access to the rewards of the other agent and estimated each other's dynamics. Both agents used a one-step model of each other to choose their optimal policy

**Method 5:** Both agent *A* and *B* had access to the rewards of the other agent and estimated each other's dynamics. Agent *A* used a two-step model of *B*, agent *B* used a one-step model of *A* to choose an optimal policy

**Method 6:** Both agent *A* and *B* had access to the rewards of the other agent and estimated each other's dynamics, and used a two-step model of each other to choose their optimal policy

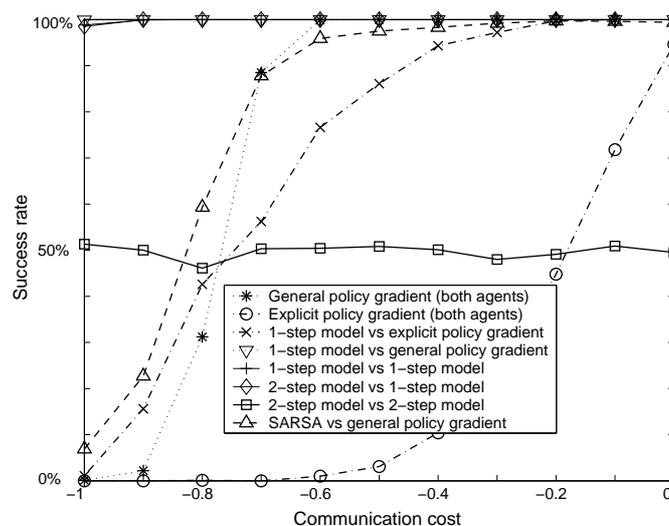


Figure 2. Performance of the various methods as a function of the cost of communication. Shorthand "vs": versus. For example, two-step vs one-step: one agent used a one-step model, the other agent used a two-step model. Note that the decrease of the explicit policy gradient and the general policy gradient curves should become steeper if the number of symbol meaning associations increases (see text).

In the experiments, the values  $\alpha$  and  $\beta$  were initialized to 0.75 in all cases. This choice enables us to compare the different methods. The values are high enough to give a fair amount of chance for the agents at the beginning to utilize communication. The values  $p_1, p_2, q_X, q_Y$  were initialized randomly according to the uniform distribution in the range  $[0.4, 0.6]$ .

In the computational studies we averaged 1000 runs. In each run we had at most 1000 learning episodes. In each episode an action was made by agent *A* and a reaction, i.e., a guess, was made by agent *B*. Learning was considered successful if after a certain number of steps, trials were 100% successful; the reward in each of the next 100 trials was +1. The number of steps needed for successful communication (not including the 100 successful ones that are used for measuring success rate) is the time needed for the agreement. Figure 2 depicts the success rate for the different methods.

The general policy gradient method (Appendix 6.2) is superior to the explicit policy gradient method (Appendix 6.1), however, if each agents uses these methods then they will not learn to communicate if communication cost is high. Value estimation based reinforcement learning methods seem to be the weakest amongst all methods that we studied (results are not shown here). Methods where agents use one-step or two-step models are sometimes 100% successful, with a single notable exception: if both agents use two-step models then success rate is only about 50%. When rewards of the other agents are available then value estimation based method (the SARSA method [6]) succeeds, too.

It can be seen, that when agents do not model each other, the chance that they learn to communicate decreases as the cost of communication increases. However, when agents model each other, they are able to learn that

communication is useful even when the cost is high, with the peculiar exception when both agents use two-step models.

Figure 3 depicts the time needed to reach an agreement. Situations when agreement was not reached are excluded from these statistics.

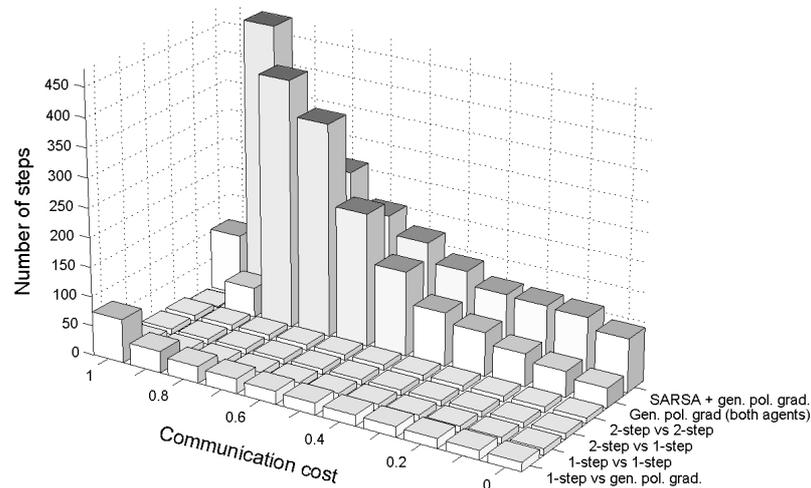


Figure 3. Learning time for various methods as a function of the cost of communication. Averages include only successful learning cases. Shorthand gen: general, pol: policy, grad: gradient

It can also be seen that when both agents can model the rewards of the other agent, then agreement about the signal-meaning association is fast. This is so, because they shortcut the slow tuning procedure of reinforcement learning: they can play the other agent's behavior "in their head", can perform the joint optimization, so they can conclude that communication is beneficial. If this shortcut is not applied, like in the case of the value estimation based SARSA method, agreement can be still reached, but only very slowly. When one of the agents thinks two steps ahead, agreement is even faster. In this case, agreement is accomplished in 1 step after an initial transient of 10 steps when the agents estimate each others' parameters. When both agents try to think two steps ahead and agreement is only achieved in 50% of the cases, agreement – if it occurs – is very fast. Thus, if agreement is not reached quickly, then agents could suspect that the second-order intentional model (e.g., one agent assumes that the other agent uses a one-step model) is not valid.

#### 4. Discussion

Theory of reinforcement learning shows that globally optimal solutions can be learned 'easily' under strict conditions. The relevant condition for us is the Markov condition: information from the past does not help in improving decisions. In other words, every information is encoded into the actual state of the agent and all state variables are amenable to the agent for acting and learning. If this condition together with some other technical assumptions are fulfilled, then the learning task is called Markov decision problem (MDP, see, e.g., [11] and the references therein).

The Markov condition is hardly met in real life. It is not met in our case either, because the parameters of decision making of agent *A* (or *B*) (i) are subject to experiences of agent *A* (or *B*), i.e., they depend on the history, (ii) these parameters are not available for agent *B* (or *A*), and (iii) agent *B* (or *A*) would benefit from knowing these parameters. In this case the world is only partially observed and task is called partially observed Markov decision problem (POMDP) (see, e.g., [5] and references therein).

This lack of information can be eased by modelling the other agent. The other agent might have many variables

and a large subset of those variables can be modelled by different means. We demonstrated this by using policy gradient methods. Both the explicit policy gradient and the general policy gradient method develop models of the ‘private’ parameters of the other agent: they model the state-action mapping, that is, the policy of the other agent. The modelling process can be explicit: a particular model is assumed in this case, or implicit, when there is a general parametrization in the policy gradient. Our simulations demonstrate that the performance of the explicit policy gradient model is inferior to that of the general model. This observation can be traced back to the differences between the methods: general policy gradient makes direct use of the immediate rewards, deals with individual state-action sequences separately. Thus, the general policy gradient method – up to some extent and indirectly – takes into account the intentions of the other agent. In the case of the model based explicit policy gradient method this connection is highly remote: the same information enters the computation only after expected value computation. Value estimation based methods (not shown here) have the same drawback and they are also inferior to the general policy gradient method. These notes concern our simple scenario that does not fulfill the conditions of MDPs.

We have shown that the lack of a single quantity, the reward, makes a huge difference: not having access to the reward of the other agent, the emergence of communication can be seriously limited if communication involves cost. The assumption that communication is costly seems realistic, because communication takes time. Without access to the rewards of the other agent, the higher the cost, the sooner the agents learn that communication is useless.

There are several exceptions to this simple observation. For example, if the policy of one of the agents is steady (i.e., this agent is not learning), then this agent will act effectively as the teacher and the adaptive agent can learn either the appropriate signal (if he is the speaker) or the appropriate meaning (if he is the listener).

The problem arises if the learning rates of the two agents are about the same. Then, to develop successful communication, they should be able to sense and then model (implicitly or explicitly) the immediate rewards, or the cumulated rewards of the other agent. Such quantities are, however, not available for the other agent. Agents can make inferences about the value of these quantities from emotional signs, such as happiness or anger. Note that the meaning of such signs can be hard to uncover. If reward related meaning of emotional signs is available for the agent and that influences the behavior of the agent, alike to human newborns, then we shall say that the agent is *emotionally coupled*. We shall say that the agents have the capability of judging and evaluating emotions of other agents and can make inferences about their rewards. It is satisfactory if one of the agents has that capability. If an agent is emotionally coupled to another agent, then the learning of symbol-meaning association may become very efficient.

It is important to note that the decrease of the explicit policy gradient and the general policy gradient curves should become much steeper if the number of symbol meaning associations increases. The reasons for this are as follows: (i) more complex situations require a larger number of communication events, (ii) the number of communication events scales with the number of possibilities, and (iii) the number of possibilities may scale with the number of variables in the exponent. For example, if an agreement is to be reached on who does what, when they do it and what will they use for doing it, then for two possible tasks, two agents, three alternative time instances, and two different tools the number of possibilities is  $3 \times 2^3 = 24$ .

There are many ways to make this learning efficient, depending on what the agents assume about their partner. Consider, for example, that both agents are emotionally coupled to each other and both agents use this when they learn to communicate. Now, it makes a huge difference how they use the emotional information they have. For example, indirect modelling of the situation occurs if we assume that the agents receive the same reward. Then we are in the MDP domain and we can apply MDP methods such as SARSA [6] – without directly modelling the other agent – safely.

A large improvement was gained if both agents considered what is the best to them. Further, if (only) one of the agents used that information to ‘anticipate’ what the other agent might prefer to do in the next step, in reaction to his action, then learning became even faster – as it was expected from theory (Section 2).

However, learning is severely spoiled if both agents are clever enough and anticipate the next step of the other agents. This has the following explanation: both agents suppose that the other is using a one-step model to model him, which, in this case, is false, because both agents use two-step models. In this situation, in 50% of the cases the randomly generated initial parameters allow to reach an agreement just by chance. In the other 50% no agreement is reached.

As we have noted earlier, in this peculiar case the agents could suspect that the one-step model they use about the other agent is false: the other agent also considers ‘what is on his partner’s mind’. Such consideration are the

starting points of game theory. However, the situation here can be different from game theory. In principle, our agents can expect very fast agreement and they can become frustrated because of the lack of this quick agreement. Our agents are also emotionally coupled and they might sense the frustration of the other agent. That is, our agents might note that their models are not valid. Thus, in our case, agents may use higher-order intentional models or they might decide whose intentions are more important and they might come to a joint agreement quickly.

Another important situation may arise if an agent is lacking the capability of emotional coupled. Such *emotionally blind* agent will have little chance to look for joint advantages and to suggest compromises. This agent has two main choices to come to agreements: it is either a supervisor (the agent is not learning) or it should be supervised (the communicating partners of the agent are not learning). Success might be severely limited if both the agent as well as the communicating partners of the agent are learning and the final result could be that the emotionally blind agent stops the communication.

An advantage of our formulation is that a new freedom appears here. The agent has the freedom to decide if he wants to optimize the sum of the two returns (cooperative agent), his own return (selfish agent), the return of the other agent no matter how much it costs (altruistic agent), might decide to change this choice, and so on. In each separate cases, agents can estimate return as well as the change of the model of the other agent. These situations call for further investigations.

In our simple example, the immediate reward and the long-term reward were identical. Situations, where these two quantities are different have also been studied. The observations are the same as in the simple case that we presented here. The only difference is that the effect of delayed reinforcement appears.

## 5. Conclusions

We have used explicit and implicit models in reinforcement learning. The world was partially observed, but otherwise it was simplified as much as possible: we used two agents, two actions and two signals. We have shown that emotional coupling is necessary for the emergence of communications even in this simplest possible case. Numerical simulations demonstrate that if the rewards of the other agent are available for modelling, then signal-meaning associations can be learned quickly. The order of intentionality agents suppose in their models about the other agent may give rise to problems, but the mere fact of the disagreement indicates that the models could be invalid. Novel situations may arise: agents might decide about their attitude towards other agents.

## Appendices: Algorithms and Pseudo Codes

### A.1 Explicit policy gradient method

In this case the explicit reward functions are available for the two agents and they can calculate the gradients of the parameter sets  $M_A = (\alpha, p_1, p_2)$  and  $M_B = (\beta, q_X, q_Y)$ :

$$R_A(M_A, M_B) = \alpha \cdot (-c_A) + 2\alpha\beta(p_1 - p_2)(q_X - q_Y)$$

for agent  $A$  and

$$R_B(M_A, M_B) = \beta \cdot (-c_B) + 2\alpha\beta(p_1 - p_2)(q_X - q_Y).$$

for agent  $B$ . As can be seen from the equations, each agent also needs to estimate the parameters of the other agent in order to calculate its own expected reward.

### A.2 General policy gradient method

Let our policy  $\pi$  depend on the parameters summarized in a vector  $\theta \in \mathbb{R}^k$ . Let  $X$  be the set of all possible trajectories in the task, and let  $r(X)$  denote the reward collected in an episode. Then  $\eta(\theta)$ , the value of the policy  $\pi(\theta)$ , is the expected value of the reward:

$$\eta(\theta) = E[r(X)] = \sum_x r(x)q(\theta, x)$$

where  $E[\cdot]$ , denotes the expectation operator,  $x \in X$  denotes a trajectory,  $r(x)$  denotes the reward collected while traversing trajectory  $x$  and  $q(\theta, x)$  is the probability of traversing trajectory  $x$  having parameters  $\theta$ . The gradient of  $\eta(\theta)$  with respect to  $\theta$  is:

Table 1. Pseudo-code of the Explicit Policy Gradient Method

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ε = 0.05, r, p ∈ [0, 1]
for each test
  α, β = 0.75, initialize p1, p2, qx, qy to random values
  for each episode i = 1, ..., MAX_EPISODES do
    Agent A
    update the approximation of the parameters of B: β̂, q̂x, q̂y
    update own parameters by gradient:
      Δα = -cA + β̂(r + p) + β̂(p1 - p2)(q̂X - q̂Y)(r - p)
      Δp1 = αβ̂(q̂X - q̂Y)(r - p)
      Δp2 = -αβ̂(q̂X - q̂Y)(r - p)
      α ← α + εΔα
      p1 ← p1 + εΔp1
      p2 ← p2 + εΔp2
    Agent B
    update the approximation of the parameters of A: α̂, p̂1, p̂2
    update own parameters by gradient:
      Δbeta = -cB + α̂(r + p) + α̂(p̂1 - p̂2)(qX - qY)(r - p)
      Δqx = α̂β(p̂1 - p̂2)(r - p)
      Δqy = -α̂β(p̂1 - p̂2)(r - p)
      β ← β + εΔβ
      qx ← qx + εΔqx
      qy ← qy + εΔqy
  end for
end for

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$$\nabla\eta(\theta) = \sum_x r(x)\nabla q(\theta, x) = \sum_x r(x) \frac{\nabla q(\theta, x)}{q(\theta, x)} q(\theta, x) = E \left[ r(X) \frac{\nabla q(\theta, X)}{q(\theta, X)} \right]$$

A sequence of trajectories  $x^1, x^2, \dots, x^n$  give an unbiased estimate of  $\nabla\eta(\theta)$ :

$$\hat{\nabla}\eta(\theta) = \frac{1}{N} \sum_{i=1}^N r(x^i) \frac{\nabla q(\theta, x^i)}{q(\theta, x^i)}$$

Because of the law of large numbers:  $\nabla\hat{\eta}(\theta) \rightarrow \nabla\eta(\theta)$  with probability 1. The quantity  $\frac{\nabla q(\theta, x)}{q(\theta, x)}$  is called likelihood ratio or score function.

Let the trajectory  $x$  be a sequence of states  $x_1, x_2, \dots, x_T$ , and let  $p_{x_t x_{t+1}}(\theta)$  be the probability of moving from state  $x_t$  to  $x_{t+1}$  having parameters  $\theta$ . Then:

$$\frac{\nabla q(\theta, x)}{q(\theta, x)} = \sum_{t=0}^{T-1} \frac{\nabla p_{x_t x_{t+1}}(\theta)}{p_{x_t x_{t+1}}(\theta)},$$

which can be derived the following way:

$$\begin{aligned} q(\theta, x) &= \prod_{t=0}^{T-1} p_{x_t x_{t+1}} \\ \Rightarrow \log q(\theta, x) &= \log \prod_{t=0}^{T-1} p_{x_t x_{t+1}} = \sum_{t=0}^{T-1} \log p_{x_t x_{t+1}} \\ \Rightarrow \nabla \log q(\theta, x) &= \sum_{t=0}^{T-1} \nabla \log p_{x_t x_{t+1}} = \sum_{t=0}^{T-1} \frac{\nabla p_{x_t x_{t+1}}}{p_{x_t x_{t+1}}}, \end{aligned}$$

Table 2. Pseudo-code for the General Policy Gradient Method

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---

```

 $z_0 = \mathbf{0} \in \mathbb{R}^k, \Delta_0 = \mathbf{0} \in \mathbb{R}^k$ 
for each episode  $j = 1, \dots, N$  do
   $R_0 = 0 \in \mathbb{R}$ 
  for each state transition  $x_t \rightarrow x_{t+1}$  do
     $z_{t+1} = z_t + \frac{\nabla p_{x_t x_{t+1}}(\theta)}{p_{x_t x_{t+1}}(\theta)}$ 
     $R_{t+1} = R_t + \frac{1}{t+1}(r_t - R_t)$ 
  end for
   $\Delta_{j+1} = \Delta_j + R_t z_t$ 
end for
 $\theta \leftarrow \theta + \frac{\Delta_N}{N}$ 

```

---



---

since  $\nabla \log f(x) = \frac{\nabla f(x)}{f(x)}$ . This sum can also be accumulated iteratively.

In our case the algorithm is simplified, since each episode consists of one step (agent  $A$  says something and agent  $B$  replies). Furthermore, we update the parameters after each episode, which means  $N = 1$  in the above algorithm. This way the two cycles boil down to one line of update after each episode:

$$\theta \leftarrow \theta + r \frac{\nabla p_{s,a}(\theta)}{p_{s,a}(\theta)}.$$

The respective gradients and probabilities can be calculated from the parameters  $\alpha, p_1, p_2, \beta, q_X, q_Y$ :

Table 3. Gradients and Probabilities for Agent  $A$ 

| state | action      | $\nabla \alpha$ | $\nabla p_1$ | $\nabla p_2$ | probability       |
|-------|-------------|-----------------|--------------|--------------|-------------------|
| 1     | X           | $p_1$           | $\alpha$     | 0            | $\alpha p_1$      |
| 1     | Y           | $1 - p_1$       | $-\alpha$    | 0            | $\alpha(1 - p_1)$ |
| 2     | X           | $p_2$           | 0            | $\alpha$     | $\alpha p_2$      |
| 2     | Y           | $1 - p_2$       | 0            | $-\alpha$    | $\alpha(1 - p_2)$ |
| *     | $\emptyset$ | -1              | 0            | 0            | $(1 - \alpha)$    |

Table 4. Gradients and Probabilities for Agent  $B$ 

| state       | action      | $\nabla \beta$ | $\nabla q_X$ | $\nabla q_Y$ | probability      |
|-------------|-------------|----------------|--------------|--------------|------------------|
| X           | 1           | $q_X$          | $\beta$      | 0            | $\beta q_X$      |
| X           | 2           | $1 - q_X$      | $-\beta$     | 0            | $\beta(1 - q_X)$ |
| Y           | 1           | $q_Y$          | 0            | $\beta$      | $\beta q_Y$      |
| Y           | 2           | $1 - q_Y$      | 0            | $-\beta$     | $\beta(1 - q_Y)$ |
| *           | $\emptyset$ | -1             | 0            | 0            | $(1 - \beta)$    |
| $\emptyset$ | 1 / 2       | 0.5            | 0            | 0            | $\beta$          |
| $\emptyset$ | $\emptyset$ | -0.5           | 0            | 0            | $(1 - \beta)$    |

In the tables the state or action denoted by  $\emptyset$  means communicating nothing.

### A.3 One-step modelling

In this case the agent calculates a conditional strategy that optimizes  $M_A$  and  $M_B$  jointly, as discussed in the text. Recall, that by joint optimization we mean that we can calculate the conditional strategy

$$M_{A|B}(M_B) = \arg \max_{M_A} R_A(M_A, M_B),$$

that is,  $A$  can calculate, that if  $B$  followed  $M_B$ , what would the optimal choice of  $A$  be.  $A$  can estimate the parameters of  $B$  and thus can estimate his policy,  $M_B = (\beta, q_X, q_Y)$ . The same is true vice versa, for agent  $B$  estimating the policy of  $A$ ,  $M_A = (\alpha, p_1, p_2)$ . The parameters can be estimated by the agents observing each other's behavior, and approximating the parameters with their relative frequencies, that is, the ratio of the occurrence frequencies of certain actions:

Table 5. Estimating Parameters

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|                                                                                                                                           |
|-------------------------------------------------------------------------------------------------------------------------------------------|
| $\hat{\alpha} = \frac{\text{\# episodes where A had chosen to communicate}}{\text{\# all episodes so far}}$                               |
| $\hat{p}_1 = \frac{\text{\# episodes where A said "X" in state "1"}}{\text{\# all episodes so far where A had chosen to communicate}}$    |
| $\hat{p}_2 = \frac{\text{\# episodes where A said "X" in state "2"}}{\text{\# all episodes so far where A had chosen to communicate}}$    |
| $\hat{\beta} = \frac{\text{\# episodes where B had chosen to listen}}{\text{\# all episodes so far}}$                                     |
| $\hat{q}_X = \frac{\text{\# episodes where B guessed "1" after hearing "X"}}{\text{\# all episodes so far where B had chosen to listen}}$ |
| $\hat{q}_Y = \frac{\text{\# episodes where B guessed "1" after hearing "Y"}}{\text{\# all episodes so far where B had chosen to listen}}$ |

---



---

Then  $M_{A|B}(M_B)$  can be derived analytically, and is the following:

- if  $B$ 's will to use communication ( $\hat{\beta}$ ) is so low that it is not worth using communication for  $A$  because of his own cost, then do not communicate anything,
- otherwise, if  $A$  is in state 1, and  $B$  is more likely to answer 1 to  $X$  than to  $Y$  ( $\hat{q}_X > \hat{q}_Y$ ), or if  $A$  is in state 2 and  $B$  is more likely to answer 2 to  $X$  than to  $Y$  ( $\hat{q}_X < \hat{q}_Y$ ), then say  $X$ ,
- otherwise say  $Y$

The conditional policy of agent  $B$ ,  $M_{B|A}(M_A)$ , is essentially the same, but using the estimated parameters of  $A$  ( $\hat{\alpha}, \hat{p}_1, \hat{p}_2$ ).

#### A.4 Two-step modelling

Supposing that  $B$  uses one-step modelling,  $A$  can think one step further. Based on that, he can simply choose his optimal strategy:

$$M_A^* = \arg \max_{M_A} R_A(M_A, M_{B|A}(M_A)).$$

This optimal policy can also be derived analytically, and is the following:

- if  $B$ 's will to use communication ( $\hat{\beta}$ ) is so low that it is not worth using communication for  $A$  because of his own cost, or  $A$ 's will to use communication ( $\hat{\alpha}$ ) is so low that it is not worth using communication for  $B$  because of his own cost, then do not communicate anything,
- otherwise, if  $A$  is in state 1, and  $\hat{p}_1 > \hat{p}_2$  (or if  $A$  is in state 2 and  $\hat{p}_1 < \hat{p}_2$ ), then suppose that  $B$  traces this, and answers 1 (2) if  $A$  says  $X$ , so say  $X$ ,
- otherwise say  $Y$

Again, the optimal policy for agent  $B$  is essentially the same, using the other's parameters.

#### A.5 SARSA

The SARSA algorithm builds a table and computes the value of each entries. For the description of the algorithm, see, e.g., [6, 7] and references therein.

Table 6. Pseudo-code of the One-step Modelling Method for Agent A

---



---

```

if  $2\hat{\beta} < c_A$ 
  do not communicate
otherwise
  if ( $A$  is in state 1 and  $\hat{q}_X > \hat{q}_Y$ ) or ( $A$  is in state 2 and  $\hat{q}_X < \hat{q}_Y$ )
    say  $X$ 
  otherwise
    say  $Y$ 
  end if
end if

```

---



---

Table 7. Pseudo-code of the Two-step Modelling Method for Agent A

---



---

```

if  $2\hat{\beta} < c_A$  or  $2\hat{\alpha} < c_B$ 
  do not communicate
otherwise
  if ( $A$  is in state 1 and  $\hat{p}_1 > \hat{p}_2$ ) or ( $A$  is in state 2 and  $\hat{p}_1 < \hat{p}_2$ )
    say  $X$ 
  otherwise
    say  $Y$ 
  end if
end if

```

---



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## References

- [1] D. P. Bertsekas and J. N. Tsitsiklis. *Neuro-Dynamic Programming*. Athena Scientific, Belmont, MA, 1996.
- [2] A. Cangelosi. Special issue on the emergence of language. *Connection Science*, Vol. 17, No. (3-4), pp. 185–397, 2005. Editor: A. Cangelosi.
- [3] R. Dunbar. *Grooming, gossip, and the evolution of language*. Harvard University Press, Cambridge, MA, 1997.
- [4] V. Gyenes, A. Bontovics, and M. Kiszlinger. “Experimenting with emotional intelligence and echo-state networks,” Technical Report ELU-November-2006-1, Eötvös Loránd University, Budapest, H, 2006. unpublished.
- [5] M. Hauskrecht. “Value-function approximations for partially observable Markov decision processes,” *Journal of Artificial Intelligence Research*, Vol. 13, pp.33–94, 2000.
- [6] G. Rummery. *Problem Solving With Reinforcement Learning*. PhD thesis, University of Cambridge, Cambridge, UK, 1995.
- [7] S. Singh, T. Jaakkola, M. L. Littman, and Cs. Szepesvári. “Convergence results for single-step on-policy reinforcement-learning algorithms,” *Machine Learning*, Vol. 38, pp. 287–303, 2000.

- [8] L. Steels. “Evolving grounded communication for robots,” *Trends in Cognitive Sciences*, Vol. 7, pp. 308–312, 2003.
- [9] L. Steels and P. Vogt. “Grounding adaptive language games in robotic agents,” In P. Harvey and P. Husbands, editors, *Proc. of European Conf. on Artificial Life*, Cambridge Ma, 1997. MIT Press. <http://www.ling.ed.ac.uk/paulv/ecal97.pdf>.
- [10] E. Stenius. “Mood and language game,” *Synthese*, Vol. 17, pp. 254–274, 1967.
- [11] R. S. Sutton and A. G. Barto. *Reinforcement Learning: An Introduction*. MIT Press, Cambridge, MA, 1998.
- [12] Sz. Számadó and E. Szathmáry. “Selective scenarios for the emergence of natural language”, *Trends in Ecology and Evolution*, 2006. (in press).
- [13] L. Wittgenstein. *Philosophical Investigations*. Basil Blackwell, Oxford, UK, 1974. Translated by G. Anscombe.



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